CSC 333 - DISCRETE STRUCTURES FOR COMPUTER SCIENCE

CREDIT HOURS: 3

PREREQUISITES: CSC 202; MTH 233 or 144

GRADE REMINDER: Must have a grade of C or better in each prerequisite course.

CATALOG DESCRIPTION

Mathematical structures for describing data, algorithms, and computing machines. Theory and application of sets, relations, functions, combinatorics, matrices, graphs, and algebraic structures which are pertinent to computer science.

PURPOSE OF COURSE

To develop logical and mathematical concepts necessary to understand and analyze computational systems. Introduce concepts, techniques, and skills necessary to comprehend the underlying structure of problems encountered in designing and implementing computer systems and software. Provide the foundations for understanding computer science topics that rely upon the comprehension of formal abstract concepts.

EDUCATIONAL OBJECTIVES

Upon successful completion of the course, students should be able to:

- 1. Use formal notation for prepositional and predicate logic.
- 2. Construct formal proofs in prepositional and predicate logic and use such proofs to determine the validity of English language arguments.
- 3. Prove conjectures using the techniques of direct proof, proof by contraposition, proof by contradiction, and proof by induction.
- 4. Prove the correctness of programs that contain looping constructs.
- 5. Demonstrate an understanding of recursive definitions and to write recursive definitions for certain sequences and collections of objects.
- 6. Describe how recursive algorithms execute.
- 7. Use set notation and set operations to prove/disprove set identities.
- 8. Use the Principle of Inclusion and Exclusion to find the number of elements in the union of sets.
- 9. Solve permutation and combination problems for a set of *n* distinct objects.
- 10. Use relations and functions and apply these concepts to ordering problems.
- 11. Use graphs, directed graphs, and trees as representation tools in a wide variety of contexts.

CONTENT	urs
Introduction to Formal Logic with applications: Logic as a model for computation e.g. the Prolog programming language Using logic as a tool to design computer components Logical expressions and circuits Design and simplification of logical expressions using Karnaugh maps Implicants and coverings of Karnaugh maps truth tables, tautologies, and the evaluation of conditional expressions in programming languages The satisfiability problem and NP-completeness Truth and provability Inference using resolution	6
Introduction to Proofs and Recurrence Relations with applications: Repetition, recursion, induction in programs Use of inductive definitions for data models Use of inductive proofs for describing error-detecting codes Proofs of program correctness Recursive definitions, e.g. parenthesized expressions Analysis of algorithms Running time of programs with iterative structures, programs with procedure calls, programs with recursive procedure calls, conditional statements Use of recurrence relations to describe running time of programs Solving recurrence relations Proving properties of programs Properties of programs that cannot be proved (unsolvable problems)	8
Sets and Combinatorics with applications:	8
The set data model Operations on sets: insert, delete, lookup Enumerative algorithms and complexity classes Algorithms for union, intersection, and difference	
Relations, Functions, and Matrices with applications: Operations on functions: insert, delete, lookup Partial orders and task system precedence constraints Total orders and execution sequencing Transitivity (pitfalls), symmetry, computing closures of relations The relational data model, keys and indexes, operations Projection and join operations Matrices as a data structure for representing relations	8
Graphs and Trees with applications: Representations of graphs using lists and matrices Paths and circuits in graphs Algorithms for detecting connected components Warshall's algorithm for reachability and transitive closure in a network Depth-first search, network broadcast patterns	8

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Use of cycle detection in file systems and concurrent systems

Applications of graph coloring: cliques, conflict scheduling

Introduction to Algebraic Structures, Languages, and Machines with applications:4

Encoding and decoding

Pattern specification and matching

Properties of regular expressions, UNIX specification of patterns

Equivalence of regular expressions and finite state automata

Minimization of automata

Graphs to represent state machines

Automata and their programs

Nondeterminism

TOTAL 45

REFERENCES

Aho, A. and Ullman, J., Foundations of Computer Science, C Edition, W.H. Freeman, 1995.

Epp, S., <u>Discrete Mathematics with Applications</u>, Cengage Learning, 2010.

Gersting, J., Mathematical Structures for Computer Science, 7th Ed., W.H. Freeman, 2014.

Grimaldi, R., <u>Discrete and Combinatorial Mathematics</u>, 5th Edition, Addison-Wesley, 2004.

Hein, J.L., Discrete Structures, Logic, and Computability, 3rd. Ed., Jones and Bartlett, 2010.